

# Blue Midnight Wish

May,12 2010

Liliya Andreicheva

# Agenda

- SHA-3 competition
- Blue Midnight Wish design
- Tweaks to the 2<sup>rd</sup> round
- Security claims
- S.Thomsen attacks
- Rotational analysis
- Conclusion
- References

# SHA-3 competition

- "NIST has opened a public competition to develop a new cryptographic hash algorithm"
- Initially 64 entries
- 1<sup>st</sup> round : 51 candidates
- 2<sup>nd</sup> round : 14 candidates

# Blue Midnight Wish(BMW)

- Authors:
  - Danilo Gligoroski, Vlastimil Klima and their team
- Norwegian University of Science and Technology
- Cryptographic hash function with output size of n-bits
- 32-bit version supports  $n \in \{224, 256\}$
- 64-bit version supports  $n \in \{384, 512\}$
- Using a block cipher of 16 rounds as part of the compression function

### Algorithm: BLUE MIDNIGHT WISH

**Input:** Message  $M$  of length  $l$  bits, and the message digest size  $n$ .

**Output:** A message digest  $Hash$ , that is  $n$  bits long.

---

#### 1. Preprocessing

- (a) Pad the message  $M$ .
- (b) Parse the padded message into  $N$ ,  $m$ -bit message blocks,  $M^{(1)}, M^{(2)}, \dots, M^{(N)}$ .
- (c) Set the initial value of the double pipe  $H^{(0)}$ .

#### 2. Hash computation

For  $i = 1$  to  $N$

{

$$Q_a^{(i)} = f_0(M^{(i)}, H^{(i-1)});$$

$$Q_b^{(i)} = f_1(M^{(i)}, H^{(i-1)}, Q_a^{(i)});$$

$$H^{(i)} = f_2(M^{(i)}, Q_a^{(i)}, Q_b^{(i)});$$

}

#### 3. Finalization

$$Q_a^{final} = f_0(H^{(N)}, CONST^{final});$$

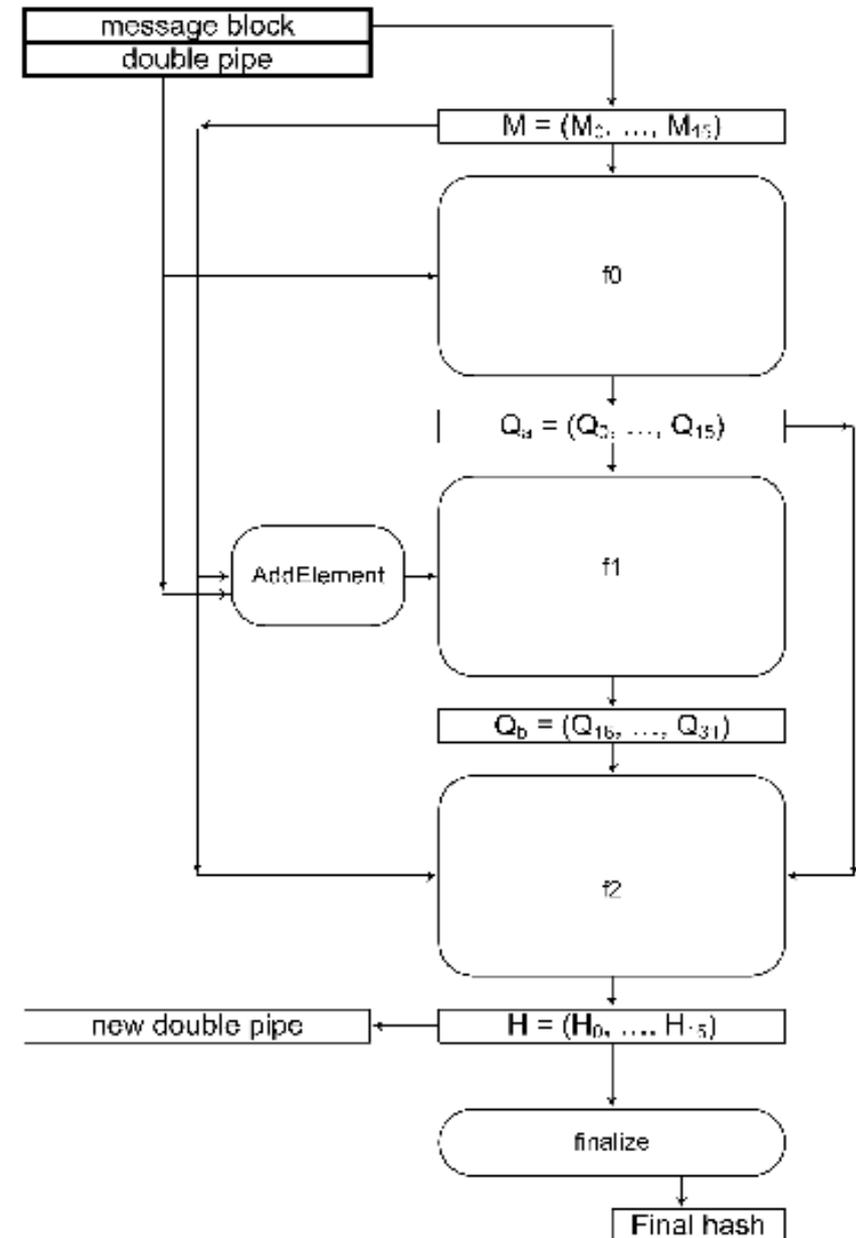
$$Q_b^{final} = f_1(H^{(N)}, CONST^{final}, Q_a^{final});$$

$$H^{final} = f_2(H^{(N)}, Q_a^{final}, Q_b^{final});$$

#### 4. $Hash = \text{Take\_}n\text{\_Least\_Significant\_Bits}(H^{final})$ .

# BMW general scheme

- $M$  – message block
- $H$  - chaining input
- $f0$  is a permutation with input  $M \text{ xor } H = Q$
- $f1$  is a multi-permutation with inputs  $M$  and  $Q$
- $f2$  is a compression on input  $M$  and  $Q$



# Tweaks to the 2<sup>nd</sup> round

- Tweaks applied to  $f_0$  and  $f_1$
- $f_0$  - rotation for chaining input H is added
- $f_1$  - chaining value H is added to the input

# Compression function : $f_0$

$$f_0 : \{0,1\}^{2m} \rightarrow \{0,1\}^m$$

**Input:** Message block  $M^{(i)} = (M_0^{(i)}, M_1^{(i)}, \dots, M_{15}^{(i)})$ , and the previous double pipe  $H^{(i-1)} = (H_0^{(i-1)}, H_1^{(i-1)}, \dots, H_{15}^{(i-1)})$ .

**Output:** First part of the quadruple pipe  $Q_a^{(i)} = (Q_0^{(i)}, Q_1^{(i)}, \dots, Q_{15}^{(i)})$ .

1. Bijective transform of  $M^{(i)} \oplus H^{(i-1)}$ :

$$\begin{aligned}
 W_0^{(i)} &= (M_5^{(i)} \oplus H_5^{(i-1)}) - (M_7^{(i)} \oplus H_7^{(i-1)}) + (M_{10}^{(i)} \oplus H_{10}^{(i-1)}) + (M_{13}^{(i)} \oplus H_{13}^{(i-1)}) + (M_{14}^{(i)} \oplus H_{14}^{(i-1)}) \\
 W_1^{(i)} &= (M_6^{(i)} \oplus H_6^{(i-1)}) - (M_8^{(i)} \oplus H_8^{(i-1)}) + (M_{11}^{(i)} \oplus H_{11}^{(i-1)}) + (M_{14}^{(i)} \oplus H_{14}^{(i-1)}) - (M_{15}^{(i)} \oplus H_{15}^{(i-1)}) \\
 W_2^{(i)} &= (M_0^{(i)} \oplus H_0^{(i-1)}) + (M_7^{(i)} \oplus H_7^{(i-1)}) + (M_9^{(i)} \oplus H_9^{(i-1)}) - (M_{12}^{(i)} \oplus H_{12}^{(i-1)}) + (M_{15}^{(i)} \oplus H_{15}^{(i-1)}) \\
 W_3^{(i)} &= (M_0^{(i)} \oplus H_0^{(i-1)}) - (M_1^{(i)} \oplus H_1^{(i-1)}) + (M_8^{(i)} \oplus H_8^{(i-1)}) - (M_{10}^{(i)} \oplus H_{10}^{(i-1)}) + (M_{13}^{(i)} \oplus H_{13}^{(i-1)}) \\
 W_4^{(i)} &= (M_1^{(i)} \oplus H_1^{(i-1)}) + (M_2^{(i)} \oplus H_2^{(i-1)}) + (M_9^{(i)} \oplus H_9^{(i-1)}) - (M_{11}^{(i)} \oplus H_{11}^{(i-1)}) - (M_{14}^{(i)} \oplus H_{14}^{(i-1)}) \\
 W_5^{(i)} &= (M_3^{(i)} \oplus H_3^{(i-1)}) - (M_2^{(i)} \oplus H_2^{(i-1)}) + (M_{10}^{(i)} \oplus H_{10}^{(i-1)}) - (M_{12}^{(i)} \oplus H_{12}^{(i-1)}) + (M_{15}^{(i)} \oplus H_{15}^{(i-1)}) \\
 W_6^{(i)} &= (M_4^{(i)} \oplus H_4^{(i-1)}) - (M_0^{(i)} \oplus H_0^{(i-1)}) - (M_3^{(i)} \oplus H_3^{(i-1)}) - (M_{11}^{(i)} \oplus H_{11}^{(i-1)}) + (M_{13}^{(i)} \oplus H_{13}^{(i-1)}) \\
 W_7^{(i)} &= (M_1^{(i)} \oplus H_1^{(i-1)}) - (M_4^{(i)} \oplus H_4^{(i-1)}) - (M_5^{(i)} \oplus H_5^{(i-1)}) - (M_{12}^{(i)} \oplus H_{12}^{(i-1)}) - (M_{14}^{(i)} \oplus H_{14}^{(i-1)}) \\
 W_8^{(i)} &= (M_2^{(i)} \oplus H_2^{(i-1)}) - (M_5^{(i)} \oplus H_5^{(i-1)}) - (M_6^{(i)} \oplus H_6^{(i-1)}) + (M_{13}^{(i)} \oplus H_{13}^{(i-1)}) - (M_{15}^{(i)} \oplus H_{15}^{(i-1)}) \\
 W_9^{(i)} &= (M_0^{(i)} \oplus H_0^{(i-1)}) - (M_3^{(i)} \oplus H_3^{(i-1)}) + (M_6^{(i)} \oplus H_6^{(i-1)}) - (M_7^{(i)} \oplus H_7^{(i-1)}) + (M_{14}^{(i)} \oplus H_{14}^{(i-1)}) \\
 W_{10}^{(i)} &= (M_8^{(i)} \oplus H_8^{(i-1)}) - (M_1^{(i)} \oplus H_1^{(i-1)}) - (M_4^{(i)} \oplus H_4^{(i-1)}) - (M_7^{(i)} \oplus H_7^{(i-1)}) + (M_{15}^{(i)} \oplus H_{15}^{(i-1)}) \\
 W_{11}^{(i)} &= (M_8^{(i)} \oplus H_8^{(i-1)}) - (M_0^{(i)} \oplus H_0^{(i-1)}) - (M_2^{(i)} \oplus H_2^{(i-1)}) - (M_5^{(i)} \oplus H_5^{(i-1)}) + (M_9^{(i)} \oplus H_9^{(i-1)}) \\
 W_{12}^{(i)} &= (M_1^{(i)} \oplus H_1^{(i-1)}) + (M_3^{(i)} \oplus H_3^{(i-1)}) - (M_6^{(i)} \oplus H_6^{(i-1)}) - (M_9^{(i)} \oplus H_9^{(i-1)}) + (M_{10}^{(i)} \oplus H_{10}^{(i-1)}) \\
 W_{13}^{(i)} &= (M_2^{(i)} \oplus H_2^{(i-1)}) + (M_4^{(i)} \oplus H_4^{(i-1)}) + (M_7^{(i)} \oplus H_7^{(i-1)}) + (M_{10}^{(i)} \oplus H_{10}^{(i-1)}) + (M_{11}^{(i)} \oplus H_{11}^{(i-1)}) \\
 W_{14}^{(i)} &= (M_3^{(i)} \oplus H_3^{(i-1)}) - (M_5^{(i)} \oplus H_5^{(i-1)}) + (M_8^{(i)} \oplus H_8^{(i-1)}) - (M_{11}^{(i)} \oplus H_{11}^{(i-1)}) - (M_{12}^{(i)} \oplus H_{12}^{(i-1)}) \\
 W_{15}^{(i)} &= (M_{12}^{(i)} \oplus H_{12}^{(i-1)}) - (M_4^{(i)} \oplus H_4^{(i-1)}) - (M_6^{(i)} \oplus H_6^{(i-1)}) - (M_9^{(i)} \oplus H_9^{(i-1)}) + (M_{13}^{(i)} \oplus H_{13}^{(i-1)})
 \end{aligned}$$

2. Further bijective transform of  $W_j^{(i)}, j = 0, \dots, 15$ :

$$\begin{aligned}
 Q_0^{(i)} &= s_0(W_0^{(i)}) + H_1^{(i-1)}; & Q_1^{(i)} &= s_1(W_1^{(i)}) + H_2^{(i-1)}; & Q_2^{(i)} &= s_2(W_2^{(i)}) + H_3^{(i-1)}; & Q_3^{(i)} &= s_3(W_3^{(i)}) + H_4^{(i-1)}; \\
 Q_4^{(i)} &= s_4(W_4^{(i)}) + H_5^{(i-1)}; & Q_5^{(i)} &= s_0(W_5^{(i)}) + H_6^{(i-1)}; & Q_6^{(i)} &= s_1(W_6^{(i)}) + H_7^{(i-1)}; & Q_7^{(i)} &= s_2(W_7^{(i)}) + H_8^{(i-1)}; \\
 Q_8^{(i)} &= s_3(W_8^{(i)}) + H_9^{(i-1)}; & Q_9^{(i)} &= s_4(W_9^{(i)}) + H_{10}^{(i-1)}; & Q_{10}^{(i)} &= s_0(W_{10}^{(i)}) + H_{11}^{(i-1)}; & Q_{11}^{(i)} &= s_1(W_{11}^{(i)}) + H_{12}^{(i-1)}; \\
 Q_{12}^{(i)} &= s_2(W_{12}^{(i)}) + H_{13}^{(i-1)}; & Q_{13}^{(i)} &= s_3(W_{13}^{(i)}) + H_{14}^{(i-1)}; & Q_{14}^{(i)} &= s_4(W_{14}^{(i)}) + H_{15}^{(i-1)}; & Q_{15}^{(i)} &= s_0(W_{15}^{(i)}) + H_0^{(i-1)};
 \end{aligned}$$

# Compression function : $f_1$

$$f_1 : \{0,1\}^{3m} \rightarrow \{0,1\}^m$$

---

**Input:** Message block  $M^{(i)} = (M_0^{(i)}, M_1^{(i)}, \dots, M_{15}^{(i)})$ , the previous double pipe  $H^{(i-1)} = (H_0^{(i-1)}, H_1^{(i-1)}, \dots, H_{15}^{(i-1)})$  and the first part of the quadruple pipe  $Q_a^{(i)} = (Q_0^{(i)}, Q_1^{(i)}, \dots, Q_{15}^{(i)})$ .

**Output:** Second part of the quadruple pipe  $Q_b^{(i)} = (Q_{16}^{(i)}, Q_{17}^{(i)}, \dots, Q_{31}^{(i)})$ .

---

1. Double pipe expansion according to the tunable parameters  $ExpandRounds_1$  and  $ExpandRounds_2$ .

1.1 For  $ii = 0$  to  $ExpandRounds_1 - 1$

$$Q_{ii+16}^{(i)} = expand_1(ii + 16)$$

1.2 For  $ii = ExpandRounds_1$  to  $ExpandRounds_1 + ExpandRounds_2 - 1$

$$Q_{ii+16}^{(i)} = expand_2(ii + 16)$$

$$s_0(x) = SHR^1(x) \oplus SHL^3(x) \oplus ROTL^4(x) \oplus ROTL^{19}(x)$$

$$s_1(x) = SHR^1(x) \oplus SHL^2(x) \oplus ROTL^8(x) \oplus ROTL^{23}(x)$$

$$s_2(x) = SHR^2(x) \oplus SHL^1(x) \oplus ROTL^{12}(x) \oplus ROTL^{25}(x)$$

$$s_3(x) = SHR^2(x) \oplus SHL^2(x) \oplus ROTL^{15}(x) \oplus ROTL^{29}(x)$$

$$s_4(x) = SHR^1(x) \oplus x$$

$$s_5(x) = SHR^2(x) \oplus x$$

$$r_1(x) = ROTL^3(x)$$

$$r_2(x) = ROTL^7(x)$$

$$r_3(x) = ROTL^{13}(x)$$

$$r_4(x) = ROTL^{16}(x)$$

$$r_5(x) = ROTL^{19}(x)$$

$$r_6(x) = ROTL^{23}(x)$$

$$r_7(x) = ROTL^{27}(x)$$

$$AddElement(j) = \left( ROTL^{(j+1)}(M_j^{(i)}) + ROTL^{(j+4)}(M_{j+3}^{(i)}) \right. \\ \left. - ROTL^{(j+11)}(M_{j+10}^{(i)}) + K_{j+16} \right) \oplus H_{j+7}^{(i)}$$

$$expand_1(j) = s_1(Q_{j-16}^{(i)}) + s_2(Q_{j-15}^{(i)}) + s_3(Q_{j-14}^{(i)}) + s_0(Q_{j-13}^{(i)}) \\ + s_1(Q_{j-12}^{(i)}) + s_2(Q_{j-11}^{(i)}) + s_3(Q_{j-10}^{(i)}) + s_0(Q_{j-9}^{(i)}) \\ + s_1(Q_{j-8}^{(i)}) + s_2(Q_{j-7}^{(i)}) + s_3(Q_{j-6}^{(i)}) + s_0(Q_{j-5}^{(i)}) \\ + s_1(Q_{j-4}^{(i)}) + s_2(Q_{j-3}^{(i)}) + s_3(Q_{j-2}^{(i)}) + s_0(Q_{j-1}^{(i)}) \\ + AddElement(j-16)$$

$$expand_2(j) = Q_{j-16}^{(i)} + r_1(Q_{j-15}^{(i)}) + Q_{j-14}^{(i)} + r_2(Q_{j-13}^{(i)}) \\ + Q_{j-12}^{(i)} + r_3(Q_{j-11}^{(i)}) + Q_{j-10}^{(i)} + r_4(Q_{j-9}^{(i)}) \\ + Q_{j-8}^{(i)} + r_5(Q_{j-7}^{(i)}) + Q_{j-6}^{(i)} + r_6(Q_{j-5}^{(i)}) \\ + Q_{j-4}^{(i)} + r_7(Q_{j-3}^{(i)}) + s_4(Q_{j-2}^{(i)}) + s_5(Q_{j-1}^{(i)}) \\ + AddElement(j-16)$$

$$s_0(x) = SHR^1(x) \oplus SHL^3(x) \oplus ROTL^4(x) \oplus ROTL^{37}(x)$$

$$s_1(x) = SHR^1(x) \oplus SHL^2(x) \oplus ROTL^{13}(x) \oplus ROTL^{43}(x)$$

$$s_2(x) = SHR^2(x) \oplus SHL^1(x) \oplus ROTL^{19}(x) \oplus ROTL^{53}(x)$$

$$s_3(x) = SHR^2(x) \oplus SHL^2(x) \oplus ROTL^{28}(x) \oplus ROTL^{59}(x)$$

$$s_4(x) = SHR^1(x) \oplus x$$

$$s_5(x) = SHR^2(x) \oplus x$$

$$r_1(x) = ROTL^5(x)$$

$$r_2(x) = ROTL^{11}(x)$$

$$r_3(x) = ROTL^{27}(x)$$

$$r_4(x) = ROTL^{32}(x)$$

$$r_5(x) = ROTL^{37}(x)$$

$$r_6(x) = ROTL^{43}(x)$$

$$r_7(x) = ROTL^{53}(x)$$

$$AddElement(j) = \left( ROTL^{(j+1)}(M_j^{(i)}) + ROTL^{(j+4)}(M_{j+3}^{(i)}) \right. \\ \left. - ROTL^{(j+11)}(M_{j+10}^{(i)}) + K_{j+16} \right) \oplus H_{j+7}^{(i)}$$

$$expand_1(j) = s_1(Q_{j-16}^{(i)}) + s_2(Q_{j-15}^{(i)}) + s_3(Q_{j-14}^{(i)}) + s_0(Q_{j-13}^{(i)}) \\ + s_1(Q_{j-12}^{(i)}) + s_2(Q_{j-11}^{(i)}) + s_3(Q_{j-10}^{(i)}) + s_0(Q_{j-9}^{(i)}) \\ + s_1(Q_{j-8}^{(i)}) + s_2(Q_{j-7}^{(i)}) + s_3(Q_{j-6}^{(i)}) + s_0(Q_{j-5}^{(i)}) \\ + s_1(Q_{j-4}^{(i)}) + s_2(Q_{j-3}^{(i)}) + s_3(Q_{j-2}^{(i)}) + s_0(Q_{j-1}^{(i)}) \\ + AddElement(j-16)$$

$$expand_2(j) = Q_{j-16}^{(i)} + r_1(Q_{j-15}^{(i)}) + Q_{j-14}^{(i)} + r_2(Q_{j-13}^{(i)}) \\ + Q_{j-12}^{(i)} + r_3(Q_{j-11}^{(i)}) + Q_{j-10}^{(i)} + r_4(Q_{j-9}^{(i)}) \\ + Q_{j-8}^{(i)} + r_5(Q_{j-7}^{(i)}) + Q_{j-6}^{(i)} + r_6(Q_{j-5}^{(i)}) \\ + Q_{j-4}^{(i)} + r_7(Q_{j-3}^{(i)}) + s_4(Q_{j-2}^{(i)}) + s_5(Q_{j-1}^{(i)}) \\ + AddElement(j-16)$$

# Compression function: $f_2$

Folding $f_2 : \{0,1\}^{3m} \rightarrow \{0,1\}^m$				
<b>Input:</b> Message block $M^{(i)} = (M_0^{(i)}, M_1^{(i)}, \dots, M_{15}^{(i)})$ ,				
quadruple pipe $Q^{(i)} = (Q_0^{(i)}, Q_1^{(i)}, \dots, Q_{15}^{(i)}, Q_{16}^{(i)}, \dots, Q_{31}^{(i)})$ .				
<b>Output:</b> New double pipe $H^{(i)} = (H_0^{(i)}, H_1^{(i)}, \dots, H_{15}^{(i)})$ .				
1. Compute the cumulative temporary variables $XL$ and $XH$ .				
	$XL =$	$Q_{16}^{(i)} \oplus Q_{17}^{(i)} \oplus \dots \oplus Q_{23}^{(i)}$		
	$XH = XL \oplus$	$Q_{24}^{(i)} \oplus Q_{25}^{(i)} \oplus \dots \oplus Q_{31}^{(i)}$		
2. Compute the new double pipe $H^{(i)}$ :				
$H_0^{(i)} =$	$(SHL^5(XH) \oplus SHR^5(Q_{16}^{(i)}) \oplus M_0^{(i)})$	$+$	$(XL \oplus Q_{24}^{(i)} \oplus Q_0^{(i)})$	
$H_1^{(i)} =$	$(SHR^7(XH) \oplus SHL^8(Q_{17}^{(i)}) \oplus M_1^{(i)})$	$+$	$(XL \oplus Q_{25}^{(i)} \oplus Q_1^{(i)})$	
$H_2^{(i)} =$	$(SHR^5(XH) \oplus SHL^5(Q_{18}^{(i)}) \oplus M_2^{(i)})$	$+$	$(XL \oplus Q_{26}^{(i)} \oplus Q_2^{(i)})$	
$H_3^{(i)} =$	$(SHR^1(XH) \oplus SHL^5(Q_{19}^{(i)}) \oplus M_3^{(i)})$	$+$	$(XL \oplus Q_{27}^{(i)} \oplus Q_3^{(i)})$	
$H_4^{(i)} =$	$(SHR^3(XH) \oplus Q_{20}^{(i)} \oplus M_4^{(i)})$	$+$	$(XL \oplus Q_{28}^{(i)} \oplus Q_4^{(i)})$	
$H_5^{(i)} =$	$(SHL^6(XH) \oplus SHR^6(Q_{21}^{(i)}) \oplus M_5^{(i)})$	$+$	$(XL \oplus Q_{29}^{(i)} \oplus Q_5^{(i)})$	
$H_6^{(i)} =$	$(SHR^4(XH) \oplus SHL^6(Q_{22}^{(i)}) \oplus M_6^{(i)})$	$+$	$(XL \oplus Q_{30}^{(i)} \oplus Q_6^{(i)})$	
$H_7^{(i)} =$	$(SHR^{11}(XH) \oplus SHL^2(Q_{23}^{(i)}) \oplus M_7^{(i)})$	$+$	$(XL \oplus Q_{31}^{(i)} \oplus Q_7^{(i)})$	
$H_8^{(i)} = ROTL^9(H_4^{(i)})$	$+$	$(XH \oplus Q_{24}^{(i)} \oplus M_8^{(i)})$	$+$	$(SHL^8(XL) \oplus Q_{23}^{(i)} \oplus Q_8^{(i)})$
$H_9^{(i)} = ROTL^{10}(H_5^{(i)})$	$+$	$(XH \oplus Q_{25}^{(i)} \oplus M_9^{(i)})$	$+$	$(SHR^6(XL) \oplus Q_{16}^{(i)} \oplus Q_9^{(i)})$
$H_{10}^{(i)} = ROTL^{11}(H_6^{(i)})$	$+$	$(XH \oplus Q_{26}^{(i)} \oplus M_{10}^{(i)})$	$+$	$(SHL^6(XL) \oplus Q_{17}^{(i)} \oplus Q_{10}^{(i)})$
$H_{11}^{(i)} = ROTL^{12}(H_7^{(i)})$	$+$	$(XH \oplus Q_{27}^{(i)} \oplus M_{11}^{(i)})$	$+$	$(SHL^4(XL) \oplus Q_{18}^{(i)} \oplus Q_{11}^{(i)})$
$H_{12}^{(i)} = ROTL^{13}(H_0^{(i)})$	$+$	$(XH \oplus Q_{28}^{(i)} \oplus M_{12}^{(i)})$	$+$	$(SHR^3(XL) \oplus Q_{19}^{(i)} \oplus Q_{12}^{(i)})$
$H_{13}^{(i)} = ROTL^{14}(H_1^{(i)})$	$+$	$(XH \oplus Q_{29}^{(i)} \oplus M_{13}^{(i)})$	$+$	$(SHR^4(XL) \oplus Q_{20}^{(i)} \oplus Q_{13}^{(i)})$
$H_{14}^{(i)} = ROTL^{15}(H_2^{(i)})$	$+$	$(XH \oplus Q_{30}^{(i)} \oplus M_{14}^{(i)})$	$+$	$(SHR^7(XL) \oplus Q_{21}^{(i)} \oplus Q_{14}^{(i)})$
$H_{15}^{(i)} = ROTL^{16}(H_3^{(i)})$	$+$	$(XH \oplus Q_{31}^{(i)} \oplus M_{15}^{(i)})$	$+$	$(SHR^2(XL) \oplus Q_{22}^{(i)} \oplus Q_{15}^{(i)})$

# Security claims

- Collision resistance of approximately bits,  $n/2$
- Preimage resistance of approximately  $n$  bits
- Second-preimage resistance of approximately  $n - k$  bits for any message shorter than  $2^k$  bits
- Resistance to length-extension attacks
- Resistance to multicollision attacks

# S.Thomsen attacks

- Pseudo-cryptanalysis on original BMW
- Showed the scenario how to attack BMW with the following complexities:
  - Near-collision attack  $2^{14}$
  - Pseudo-collision attack  $2^{(3n/8 + 1)}$
  - Pseudo-(second) preimage attack  $2^{(3n/4+1)}$

where  $n$  is the length of the input

# S.Thomsen attacks(cont.)

- Near-collision attacks
  - The strategy is to search for difference patterns of the last few words of  $W$ , such that these differences do not spread too much in the last few rounds of  $f_1$  and  $f_2$
- Pseudo attacks
  - The idea is to fix some of the output words  $Q(16, \dots, 31)$ , then  $f_2$  becomes simple. Thus fixing one of the input value attacker is controlling some of the words of chaining input  $H$ .

# S.Thomsen attacks(cont.)

- Complexity:
  - Controlling 2 output words:
    - Pseudo-collision attack  $2^{(7n/16)}$
    - Pseudo-preimage attack  $2^{(7n/8)}$
  - Controlling 4 output words:
    - Pseudo-collision attack  $2^{(3n/8 + 1)}$
    - Pseudo-preimage attack  $2^{(3n/4 + 1)}$

---

Variant	Pseudo-collision	Pseudo-(second) preimage
BMW-224	$2^{81} (2^{112})$	$2^{161} (2^{224})$
BMW-256	$2^{97} (2^{128})$	$2^{193} (2^{256})$
BMW-384	$2^{128} (2^{192})$	$2^{256} (2^{384})$
BMW-512	$2^{192} (2^{256})$	$2^{384} (2^{512})$

---

# Rotational analysis

- Relatively new type of analysis
- Looking at the propagation of rotational pair((x,x <<<r)) through some transformation.
- Rotational input produces rotational output with some probability
- Reduces the complexity of obtaining the original message
- BMW-512 :  $2^{223.5}$

# Conclusion

- Attacks presented by Thomsen are infeasible
- Further investigation concerning rotational analysis is needed

# References

- Soren S. Thomsen - Pseudo-cryptanalysis of Blue Midnight Wish. Available online, 2009
- Jian Guo, Soen S. Thomsen - Distinguishers for the Compression Function of Blue Midnight Wish with Probability 1. Available online, 2010
- Soren S. Thomsen - Pseudo-cryptanalysis of the Original Blue Midnight Wish. In S.Hong and T.Iwata, editors, Fast Software Encryption, LNCS, Seoul, South Korea, 2010. To appear
- Ivica Nikolic, Josef Pieprzyk, Przemyslaw Sokolowski, Ron Steinfeld - Rotational Cryptanalysis of (Modified) Versions of BMW and SIMD. Available online, 2010 Soren S. Thomsen - A near-collision attack on the Blue Midnight Wish compression function. Version 2.0, available online, 2008

Thank you!

Questions?