# Supersingular Isogeny Key Encapsulation

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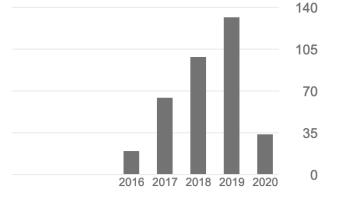
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# Isogeny

From Wikipedia, the free encyclopedia

In mathematics, in particular, in algebraic geometry, an **isogeny** is a morphism of algebraic groups (a.k.a group varieties) that is surjective and has a finite kernel.

If the groups are abelian varieties, then any morphism  $f: A \to B$  of the underlying algebraic varieties which is surjective with finite fibres is automatically an isogeny, provided that  $f(1_A) = 1_B$ . Such an isogeny f then provides a group homomorphism between the groups of k-valued points of A and B, for any field k over which f is defined.

The terms "isogeny" and "isogenous" come from the Greek word  $\iota\sigma\circ\gamma\epsilon\nu\eta$ - $\varsigma$ , meaning "equal in kind or nature". The term "isogeny" was introduced by Weil; before this, the term "isomorphism" was somewhat confusingly used for what is now called an isogeny.

## Overview of SIDH

- 1. Public parameters: Supersingular elliptic curve E over F.
- 2. Alice chooses a kernel  $A \subset E$  and sends E/A to Bob.
- 3. Bob chooses a kernel  $B \subset E$  and sends E/B to Alice.
- 4. The shared secret is

$$E/\langle A, B \rangle = (E/A)/\phi_A(B) = (E/B)/\phi_B(A).$$

$$E \xrightarrow{\phi_A} E/A$$

$$\phi_B \downarrow \qquad \qquad \downarrow$$

$$E/B \qquad \downarrow F/A \Rightarrow F$$

# Supersingular isogeny key exchange

From Wikipedia, the free encyclopedia

Supersingular isogeny Diffie–Hellman key exchange (SIDH) is a post-quantum cryptographic algorithm used to establish a secret key between two parties over an otherwise insecure communications channel. It is analogous to the Diffie–Hellman key exchange, but is based on walks in a supersingular isogeny graph and is designed to resist cryptanalytic attack by an adversary in possession of a quantum computer. SIDH boasts one of the smallest key sizes of all post-quantum key exchanges; with compression, SIDH uses 2688-bit<sup>[1]</sup> public keys at a 128-bit quantum security level. SIDH also distinguishes itself from similar systems such as NTRU and Ring-LWE by supporting perfect forward secrecy, a property that prevents compromised long-term keys from compromising the confidentiality of old communication sessions. These properties make SIDH a natural candidate to replace Diffie–Hellman (DHE) and elliptic curve Diffie–Hellman (ECDHE), which are widely used in Internet communication.