



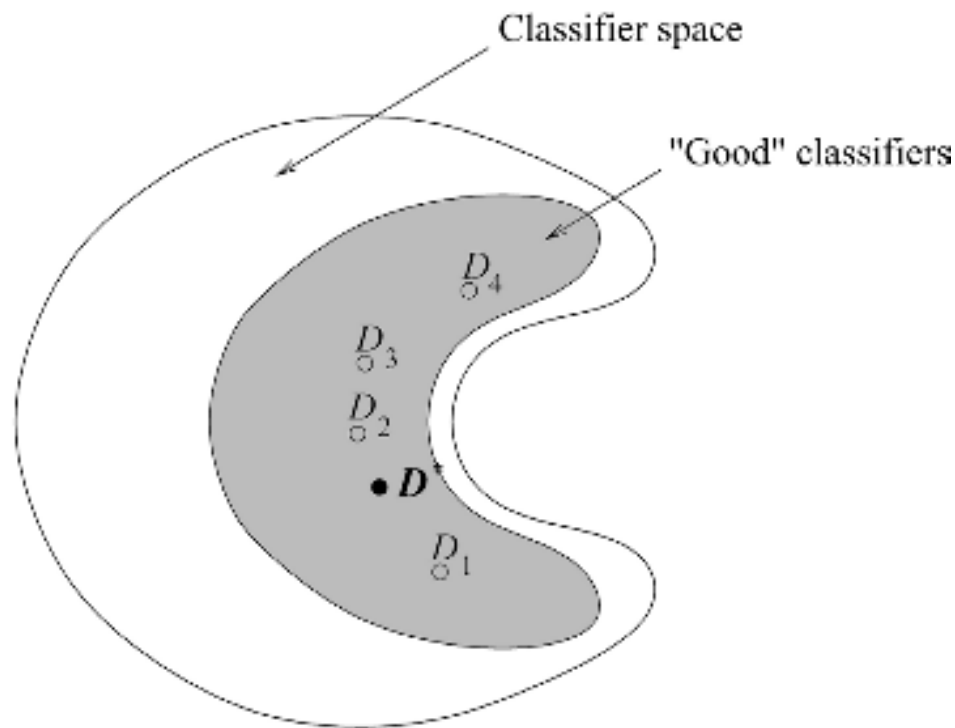
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# Classifier Combination

Kuncheva Ch. 3

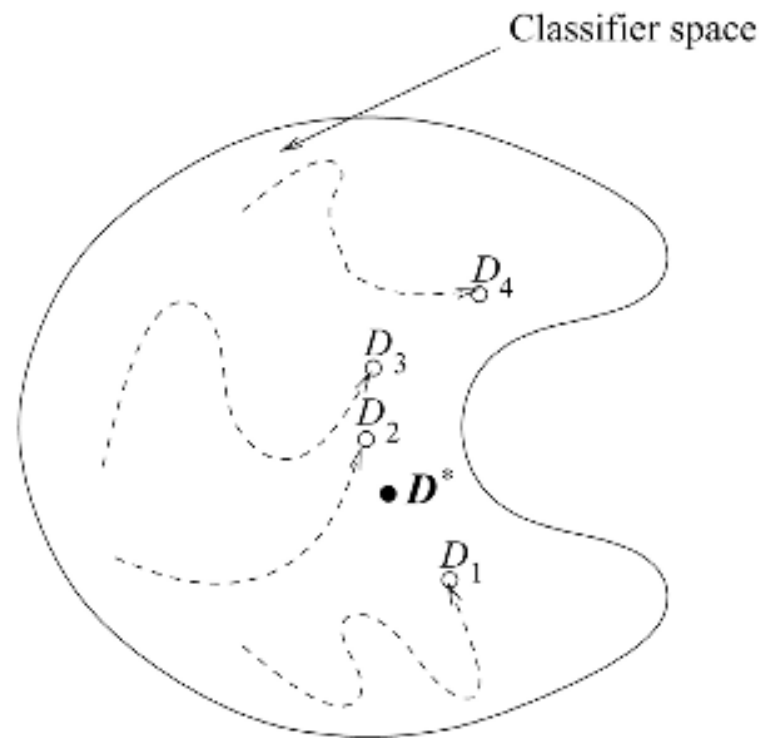
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# Combination: The Statistical Reason



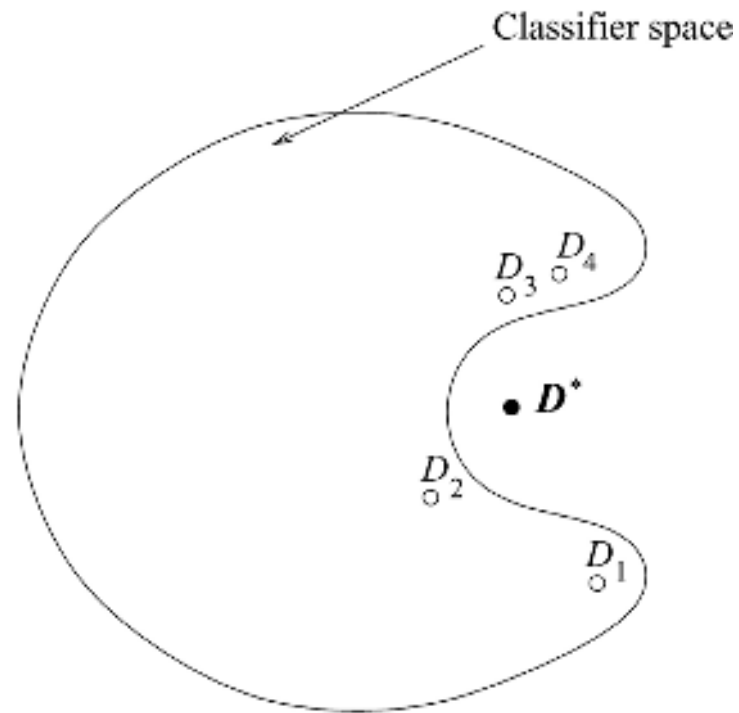
**Fig. 3.1** The statistical reason for combining classifiers.  $D^*$  is the best classifier for the problem, the outer curve shows the space of all classifiers; the shaded area is the space of classifiers with good performances on the data set.

# Combination: The Computational Reason



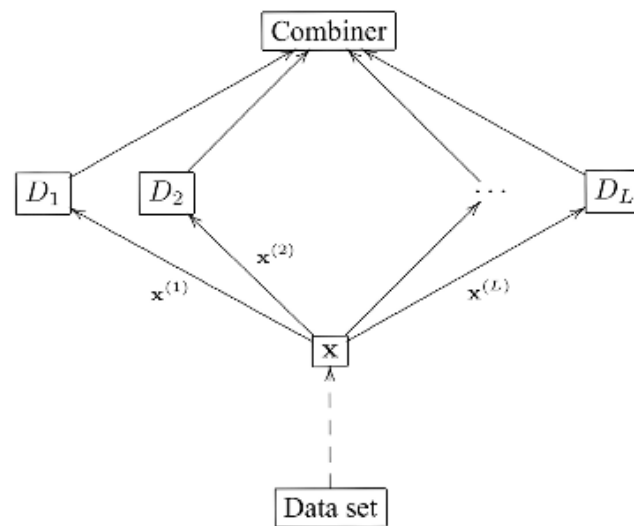
**Fig. 3.2** The computational reason for combining classifiers.  $D^*$  is the best classifier for the problem, the closed space shows the space of all classifiers, the dashed lines are the hypothetical trajectories for the classifiers during training.

# Combination: The Representational Reason



**Fig. 3.3** The representational reason for combining classifiers.  $D^*$  is the best classifier for the problem; the closed shape shows the chosen space of classifiers.

# Classifier Ensembles: Types of Combination



**A. Combination level:**  
Design different  
combiners.

**B. Classifier level:**  
Use different  
base classifiers.

**C. Feature level:**  
Use different  
feature subsets.

**D. Data level:**  
Use different  
data subsets.

*Fig. 3.4 Approaches to building classifier ensembles.*

# Training: Stacked Generalization

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	A	B	C	D
Training	B	C	D	A
	C	D	A	B
<hr/>				
Testing	D	A	B	C

*Fig. 3.5 Standard four-fold cross-validation set-up.*

## Protocol:

Train base classifiers using cross-fold validation

Then train combiner on all N points by using the class labels output by the base classifiers for each fold (train/test partition)

# Other Issues

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Fusion vs. Selection

Trainable vs. Non-trainable Combiners

Decision Optimization vs. Coverage  
Optimization

- Tuning a fixed set of base classifiers vs. creating diverse base classifiers using a fixed combiner



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# Fusion of Class Labels

Kuncheva, Ch. 4

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# Let's Start at the End...

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## 4.8 CONCLUSIONS

This chapter describes various methods for combining class label outputs. Formally speaking, we transformed the problem to find a mapping

$$D : \mathcal{R}^n \rightarrow \Omega \quad (4.82)$$

into a problem of finding a mapping

$$\mathcal{F} : \Omega^L \rightarrow \Omega \quad (4.83)$$

We can call  $\Omega^L$  an *intermediate feature space*, which in this case is discrete. The methods described here varied on the assumptions and also on the complexity of their implementation. Table 4.11 summarizes the methods in this chapter.

# Methods for Fusing Class (Label) Outputs

**TABLE 4.11 A Summary of the Label Fusion Methods.**

Method	Assumptions (for Optimality)	Memory Requirements (in Number of Parameters Needed for Its Operation)
Majority vote	None	None
Weighted majority vote	None	$L$
Naive Bayes	Conditional independence	$L \times c^2$
Behavior knowledge space (BKS)	None	$c^L$
Wernecke	None	$c^L$
First-order dependence tree	Conditional first-order dependence	$c \times [(L - 1) \times c^2 + L]$
SVD combination	None	$[L \times c + (c + 1)]\delta$ $(\delta \leq \min\{N, (L \cdot c)\})$

SVD, singular value decomposition.

# Classifier Output Types

*(Xu, Krzyzak, Suen; ad. by Kuncheva)*

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## Type 0: Oracle Level (Kuncheva)

Outputs: 0/1 (incorrect/correct)

## Type 1: Abstract Level

Outputs: Chosen class label

## Type 2: Rank Level

List of ranked class labels

## Type 3: Measurement Level

Output: (Usually) values in  $[0, 1]$  for each .class  
(discriminant function outputs)

# Simple Consensus Models

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Unanimity  
(all agree)



Simple majority  
(50%+1)



Plurality  
(most votes)



**Fig. 4.1** Consensus patterns in a group of 10 decision makers: unanimity, simple majority, and plurality. In all three cases the final decision of the group is “black.”