

$$\langle T_{zz} \rangle = -3 \times \frac{\pi^2}{1440 a^4}.$$